Pedotransfer function application for estimation of soil hydrophysical properties using parametric methods

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ABSTRACT

Soil hydraulic properties are needed as input data to describe and simulate the transport of water and solutes in the soil profile. The most important characteristics are the soil moisture retention curve (SMRC) $\theta(h)$ and the hydraulic conductivity function $k(\theta)$ or k(h), where θ is the soil moisture content, h is the pressure head and k is the hydraulic conductivity. SMRC represents the amount of water remaining in the soil under equilibrium conditions and is unique for each soil. The measurement of SMRC is laborious and time-consuming and so there are not enough data available sometimes. Various SMRC estimation models have been proposed and used extensively to overcome this problem. Other more easily available soil properties, such as particle size distribution, organic matter content, soil structure and bulk density, were used for the estimation of SMRC. Bouma and van Lanen (1987) called these models "transfer functions", and later on they were called "pedotransfer functions". This study is based on European works by Wösten et al. (1998, 1999), and others. The pedotransfer functions derived by Wösten et al. (1998) were used in the first part of the study. In the second part, the authors derived their own pedotransfer functions for the sites where all necessary data were available. The methodology of data processing was similar to that used by Wösten et al. (1998) for continuous pedotransfer functions. The use of continuous pedotransfer functions was tested on data sets from several sites in the Czech Republic (Cerhovice, Černičí, Brozany, Ovesná Lhota, Tupadly, Džbánov, Podlesí and Žichlínek). Unfortunately, the available Czech data sets are not as large as the data sets used in Wösten's work. Quite good new estimates of SMRC (expressed as pF curves) were found e.g. for the Cerhovice and Černičí sites; the estimates for a man-made soil profile in Brozany and for natural soils in Ovesná Lhota, Tupadly, Džbánov, Podlesí and Žichlínek were less successful, partly because of insufficient input data. The applications of continuous pedotransfer functions derived by Wösten et al. (1998) for the Czech data sets were not very successful, either. The quality and size of the input data sets are critical factors for a successful use of pedotransfer functions.

Keywords: soil moisture retention curve; pedotransfer function; multiple linear regressions; parametric method

Soil hydraulic properties are needed as input data to describe and simulate the transport of water and solutes in the soil profile. Two main soil hydraulic properties, being commonly considered as soil's fingerprints, are:

1. Soil-moisture retention curve (SMRC), which represents the amount of water remaining in the soil at equilibrium, expressed in terms of soil water content θ as a function of the soil water pressure head h (Hillel 1998, p. 155). The decadic logarithm of h, if h is expressed in centimeters,

- is usually denoted as pF and the relation $\theta(pF)$ is referred to as a pF curve.
- 2. Saturated hydraulic conductivity K and the unsaturated hydraulic conductivity k as a function of the soil water content or pressure head, $k(\theta)$ or k(h).

The shape of SMRC is unique for each soil. It can be determined by direct measurements and is related to many other soil properties. The measurement procedures are time consuming and laborious and, quite often, SMRC is not a part of the standard

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soil survey. Hence, various models to estimate SMRC have been proposed and extensively used. Other, more easily determinable and available soil properties, such as the particle-size distribution, organic matter content, soil structure descriptors and soil bulk density, were used for this purpose. Bouma and van Lanen (1987) called these models pedotransfer functions (PTF's).

Cornelis et al. (2001) divided PTF's into three groups:

Group 1 – estimation of soil water contents at particular suction head values by multiple linear regression (Gupta and Larson 1979, Rawls and Brakensiek 1982, Saxton et al. 1986) and/or using artificial neural networks (Pachepsky et al. 1996).

Group 2 – predicting the parameters of closed-form analytical equations, like those by Brooks and Corey (1964) (done by Rawls and Brakensiek 1985), or van Genuchten (1980). This is again achieved by multiple linear regression (Vereecken et al. 1989, Scheinost et al. 1997, Wösten et al. 1998, Minasny et al. 1999, Wösten et al. 1999) or artificial neural networks (Pachepsky et al. 1996, Schaap et al. 1998a, b, 1999, Minasny et al. 1999).

Group 3 – based on a physical-conceptual model of water retention phenomena (Arya and Paris 1981, Haverkamp and Parlange 1986) or on the use of fractal mathematics and scaled similarities (Tyler and Wheatcraft 1989, Comegna et al. 1998).

An evaluation of applicability and prediction accuracy of some most common PTF's which use other soil properties, like particle size distribution (contents of clay, sand and silt), organic matter or organic carbon content and dry bulk density as estimators, was done by Cornelis et al. (2001).

Commonly, either the regression or the artificial neural networks have been used to find the parameters of pedotransfer functions (PTF's). These methods can be called **parametric**. In some new applications, **nonparametric methods** have been successfully used. These techniques do not use any predefined mathematical functions. They work with similarities instead of fitting equations to data. Nemes et al. (2006) introduced a relatively simple form of nonparametric lazy learning algorithm, called k-Nearest Neighbor algorithm (k-NN), to estimate soil hydraulic properties, and compared the results with a neural network model.

If the soil properties to be estimated (e.g. SMRC parameters) appear in PTF's as continuous functions of the other soil properties, the PTF's are referred to as continuous.

This preliminary study is focused on SMRC and the possibility of using parametric PTF's belonging to group 2, especially those based on the works by Wösten et al. (1998), Wösten et al. (1999), and other European authors. The PTF technique is applied to selected soils from different regions of the Czech Republic. An attempt has been made to derive new pedotransfer functions for these soils and regions.

MATERIAL AND METHODS

Available data sets from several sites (Brozany, Černičí, Cerhovice, Ovesná Lhota, Tupadly, Džbánov, Podlesí and Žichlínek) were tested in this work. Basic information about these sites is summarized in Tables 1 and 2.

The continuous pedotransfer functions of Wösten et al. (1998) were used to determine the parameters of the closed-form analytical van Genuchten equation:

$$\theta(h) = \theta_r + \frac{\theta_s - \theta_r}{\left(1 + \left|\alpha h\right|^n\right)^{\left(1 - \frac{1}{2}\right)}} \qquad h < 0$$
 (1)

where:

 $\theta(h)$ = soil water content as a function of pressure head h

 θ_r = residual soil water content – a parameter

 θ_s = saturated soil water content – a parameter

 α , n = empirical parameters

In the parameterization procedure the residual soil water content θ_r was initially set to 0.01 and than later changed if measured data suggested otherwise, following the line of Wösten et al. (1998). The existing regression equations for individual parameters of the van Genuchten equation (θ_s , α^* , n^*), as determined by Wösten et al. (1998), are listed in Table 3. The R^2 values in Table 3 refer to multiple correlation between the other soil properties (independent variables) and the parameters θ_s , α^* and n^* to be estimated. Let us note that the lowest R^2 was obtained for α^* .

Firstly, the measured data points $\theta(h)$ for individual retention curves were parameterized, using the RETC computer program (van Genuchten et al. 1991) to obtain the fitted parameters θ_s , α , and n. Secondly, the continuous pedotransfer functions of Wösten et al. (1998), as given in Table 3, were used to estimate SMRC parameters for each site. Thirdly, our own continuous pedotransfer functions were derived, using the data from all sites. The technique of derivation was similar to that used by Wösten et al. (1998). The input data for

Table 1. Basic information about the sites and soils studied – part I $\,$

Site	Nearest town	Mean altitude (m a.s.l.)	Dominant soil types (FAO/ISRIC classification)	Organic matter content (%)	USDA textural triangle	
Cerhovice	Hořovice	425	Fluvi-eutric Gleysol	1.44	silt loam, silty clay loam, silty clay, clay loam	
Tupadly	Štětí (Mělník)	256	Orthic Luvisol	0.22-1.73	silty clay loam, silty clay, clay	
Brozany	Pardubice	217	Artificial soil profile, man-made, compacted and left for 3 years of consolidation, Eutric Fluvisol	e, 1.30–1.90 sand, sandy loam		
Černičí	Čechtice (Vlašim)	510	Dystric Cambisol	2.20	sandy loam	
Ovesná Lhota	Světlá nad Sázavou (Havlíčkův Brod)	528	Stagnogleyic Cambisol	na	sandy loam, loam	
Džbánov	Ústí nad Orlicí	308	Orthic Luvisol	na	silt loam	
Podlesí	Ústí nad Orlicí	380	Stagnogleyic Luvisol	na	silt loam	
Žichlínek	Ústí nad Orlicí	390	Albo-gleyic Luvisol	na	silt loam, silty clay loam	

na = data not available

Table 2. Basic information about the sites and soils studied – part $\rm II$

Site and depth of sampling (cm)	Porosity (%)	Particle density (g/cm³)	Bulk density (g/cm³)	% clay	% silt	% sand
Cerhovice 15, 30	43.0	2.27-2.76	1.30-1.60	17.6-42.1	41.8-64.9	3.6-20.3
Tupadly 15, 30, 70	41.2-45.2	2.33-2.41	1.33-1.45	38.2-48.3	35.2-46.2	15.5–16.5
Brozany 30, 50, 85	38.3-48.9	2.68-2.70	1.33-1.66	0.0-6.5	2.1-34.9	58.6-97.9
Černičí 10, 25, 30, 35, 45	42.1-65.1	2.62-2.69	1.53-1.87	9.6	21.9	68.5
Ovesná Lhota 20, 40, 60, 80	37.0-49.0	2.34-2.75	1.30-1.58	8.3–19.7	637.3	51.2-75.2
Džbánov 15, 30, 55, 80, 130	39.4–45.9	2.67-2.74	1.45-1.62	18.5-25.3	52.5-60.0	19.2–25.1
Podlesí 10, 35, 70, 95	41.2-44.1	2.63-2.72	1.48-1.59	9.0-23.4	54.6-66.0	18.3-25.0
Žichlínek 20, 45, 75, 120	36.5-48.1	2.66-2.74	1.38-1.74	11.2-24.7	15.3-30.8	49.4-57.2

Table 3. Continuous pedotransfer functions according to Wösten et al. (1998)

Equations for model parameters of van Genuchten's equations	R^{2} (%)
$\theta_s = 0.7919 + 0.001691 \times C - 0.29619 \times D - 0.000001491 \times S^2 + 0.0000821 \times OM^2 + 0.02427 \times C^{-1} + 0.01113 \times S^{-1} + 0.01472 \times \ln(S) - 0.0000733 \times OM \times C - 0.000619 \times D \times C - 0.001183 \times D \times OM - 0.0001664 \times \text{topsoil} \times S$	76
$\begin{array}{l} \alpha^* = -14.96 + 0.03135 \times C + 0.0351 \times S + 0.646 \times OM + 15.29 \times D - 0.192 \times topsoil \\ -4.671 \times D^2 - 0.000781 \times C^2 - 0.00687 \times OM^2 + 0.0449 \times OM^{-1} + 0.0663 \times ln(S) + 0.1482 \times ln(OM) \\ -0.04546 \times D \times S - 0.4852 \times D \times OM + 0.00673 \times topsoil \times C \end{array}$	20
$n^* = -25.23 - 0.02195 \times C + 0.0074 \times S - 0.1940 \times OM + 45.5 \times D - 7.24 \times D^2 + 0.0003658 \times C^2 + 0.002885 \times OM - 12.81 \times D^{-1} - 0.1524 \times S^{-1} - 0.01958 \times OM^{-1} - 0.2876 \times \ln(S) - 0.0709 \times \ln(OM) - 44.6 \times \ln(D) - 0.02264 \times D \times C + 0.0896 \times D \times OM + 0.00718 \times \text{topsoil} \times C$	54

 θ_s = saturated soil water content – a parameter; α^* , n^* = transformed model parameters: α^* = lna, n^* = ln(n-1); C = % clay $(0-2 \mu m)$; S = % silt $(2-50 \mu m)$; OM = % organic matter; D = dry bulk density $(= \rho_d)$ (Mg/m³ or g/cm³); topsoil = a qualitative parameter (1 for topsoil, 0 for subsoil); ln = natural logarithm

our own pedotransfer functions were the particlesize distribution (percentage of sand, silt, and clay), organic matter content, dry bulk density and a qualitative parameter equal to 1 for topsoil and 0 for subsoil. The original particle-size distribution data (expressed in terms of particle size categories currently used in the Czech Republic) were converted to the FAO/USDA categories. The coefficients of these functions were obtained by multiple regression (using the program Statistica CZ), relating these input data to the individually fitted parameters θ_s , α^* , and n^* . Fourthly, for the sites where there were enough measured retention data (Brozany, Cerhovice, Černičí and Ovesná Lhota), particular pedotransfer functions were derived in the same manner.

The quality of newly estimated retention curves was evaluated using the \mathbb{R}^2 coefficient for correlation between the measured and the estimated soil

Table 4. Results of evaluation of different pedotransfer functions for SMRC estimation based on large data sets (Tietje and Tapkenhinrichs 1993)

Reference	RMSD (m^3/m^3)			
Gupta and Larson (1979)	0.0591			
Arya and Paris (1981)	0.0611			
Rawls and Brakensiek (1985)	0.0751			
Vereecken et al. (1989)	0.0531			
Tyler and Wheatcraft (1989)	0.0768			

RMSD is an average of the Root of the Mean Squared Difference between predicted and measured soil water contents at different pF values

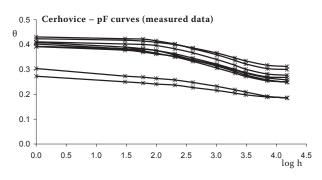
water content at several pF values, as in Wösten et al. (1998), and RMSD (Root of the Mean Squared Difference). Table 4 presents, for comparison, the RMSD values for large data sets published by Tietje and Tapkenhinrichs (1993). The R^2 coefficients for correlation between the individually derived and the globally fitted parameters θ_s , α , and n were also calculated. In addition, all pF curves were plotted into graphs for a visual comparison.

RESULTS AND DISCUSSION

The measured SMRC, expressed as pF curves, and their individually parameterized counterparts corresponded very well to one another, except for the Brozany site and for the points nearest to saturation. This is documented not only by high R^2 and low RMSD values in Table 6, but also by a visual comparison of the curves (an example for the Cerhovice site is given in Figure 1). Hence, the van Genuchten equation (1) is reasonably suitable for expressing the retention curves of many Czech soils and the RETC software used (van Genuchten et al. 1991) works well with these soils.

On the other hand, the application of pedotransfer functions by Wösten et al. (1998) to our data was not very successful. RMSD in more successful cases ranged between 0.0591 and 0.0790, but in other cases RMSD values between 0.1113 and 0.2391 were found (see Table 6, column "Obs. vs. Wösten" for RMSD).

The pedotransfer functions for θ_s , α^* and n^* , newly derived from the data of all sites taken to-



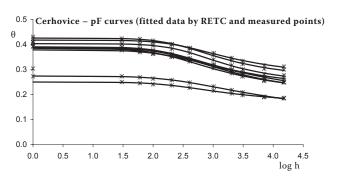


Figure 1. Comparison of observed and fitted (using RETC software) pF curves (the measured points are indicated in both graphs)

gether (see Table 5), did not fit the observed curves very well. An acceptably good fit was obtained for Cerhovice, Džbánov, Podlesí and Žichlínek (RMSD ranged between 0.0591 and 0.0790), but the RMSD values for Brozany, Černičí, Ovesná Lhota and Tupadly lay between 0.1113 and 0.3143, which indicates a very poor agreement with the observed data. The R^2 values in Table 5 refer to multiple correlation between the other soil properties (independent variables) and the parameters θ_s , α^* and n^* to be estimated. In contrary to Table 3, it is now mainly the saturated soil water content θ_s for which the R^2 value is extremely low, indicating a poor correlation.

Particular pedotransfer functions were derived for Brozany, Cerhovice, Černičí and Ovesná Lhota. The estimates for Cerhovice and Černičí were successful, RMSD being 0.0519 and 0.0451, respectively (see Table 6), which is less than the values obtained for large data sets by Tietje and Tapkenhinrichs (1993), with PTF's according to Vereecken et al. (1989), Rawls and Brakensiek (1985), and other authors (Table 4). On the other hand, RMSD for Brozany and Ovesná Lhota were 0.3874 and 0.2149, respectively, which indicates that even the site-specific PTF's do not explain the

data well enough. In the case of Brozany, we can even say that the van Genuchten equation per se does not fit the measured retention curves at all, as indicated by the high value of RMSD for the correlation between the measured and individually fitted soil water contents (0.3397). In this context, it has to be mentioned that Brozany soil profile is a man-made soil profile in a giant lysimeter, compacted and left for three years to consolidate before the sampling. In the case of Ovesná Lhota, a partial explanation of the failure may be that the available data set is rather old and incomplete.

To assess the quality of the estimated curves, R^2 coefficients for correlation between the parameters θ_s , α and n derived for each soil sample from site-specific PTF's and those obtained by fitting each curve individually (using RETC) are given in Table 7. The very low values of R^2 (except for Černičí) show that the fit was not very good.

When judging various methods of quantifying the adequacy and accuracy of the estimated retention curves, RMSD for correlation between the measured and estimated soil water contents at several different pF values seems to be the best option. This opinion of the authors is supported by Kobayashi and Us Salam (2000), who prefer

Table 5. Newly derived continuous pedotransfer functions (for all sites together)

Equations for model parameters of van Genuchten's equations	R ² (%)
$\begin{array}{l} \theta_s = 0.75608 + 0.05616 \times C + 0.11152 \times D + 0.00003 \times S^2 + 0.00423 \times OM^2 \\ + 0.29552 \times C^{-1} - 1.55257 \times S^{-1} - 0.12207 \times \ln(S) + 0.02102 \times OM \times C \\ - 0.04672 \times D \times C - 0.08348 \times D \times OM - 0.00031 \times \text{topsoil} \times S \end{array}$	29
$\alpha^* = -103.709 - 0.287 \times C + 0.092 \times S + 47.929 \times OM + 98.173 \times D + 4.019 \times topsoil \\ -37.314 \times D^2 + 0.001 \times C^2 - 13.943 \times OM^2 + 18.577 \times OM^{-1} \\ -5.625 \times ln(S) + 0.155 \times OM \times D$	82
$\begin{split} n^* &= 7.0186 + 0.0595 \times \text{C} - 0.0133 \times \text{S} - 2.0409 \times \text{OM} + 18.6714 \times \text{D} \\ &- 15.1404 \times \text{D}^2 - 0.0007 \times \text{C}^2 - 19.9935 \times \text{D}^{-1} + 10.7434 \times \text{S}^{-1} - 0.8598 \times \text{OM}^{-1} \\ &+ 1.3763 \times \ln(\text{S}) - 4.3084 \times \ln(\text{OM}) + 6.1984 \times \ln(\text{D}) + 3.5008 \times \text{D} \times \text{OM} - 0.0214 \times \text{topsoil} \times \text{C} \end{split}$	83

Table 6. Goodness-of-fit indicators (R^2 and RMSD) for different cases

	No. of SMRC fitted	\mathbb{R}^2 coefficient			RMSD (m ³ /m ³)				
Site		Obs. vs. fitted	Obs. vs. Wösten	Obs. vs. newly derived PTF's	Obs. vs. own total PTF's	Obs. vs. fitted	Obs. vs. Wösten	Obs. vs. newly derived PTF's	Obs. vs. own total PTF's
Brozany	8	98.48	86.28	62.12	75.76	0.3397	0.2391	0.3874	0.3240
Cerhovice	9	98.35	95.70	95.30	73.49	0.0421	0.0627	0.0519	0.9178
Černičí	10	93.87	84.96	93.35	93.27	0.0432	0.2404	0.0451	0.2439
Ovesná Lhota	8	90.66	89.49	93.02	87.49	0.1413	0.3143	0.2149	0.1780
Tupadly	3	91.90	89.95	na	82.30	0.1043	0.1113	na	0.1667
Džbánov	4	97.92	79.37	na	77.51	0.0800	0.0591	na	0.1961
Podlesí	4	99.55	81.77	na	77.92	0.0996	0.0790	na	0.2293
Žichlínek	3	98.94	79.82	na	74.21	0.1044	0.0705	na	0.3652

na = not applicable due to the lack of input data

the RMSD evaluation to the squared correlation coefficients (R^2) for quantifying the accuracy of the estimated data.

For a visual comparison, graphs of concomitant pF curves were plotted. Examples for Cerhovice and Černičí are depicted in Figures 2 and 3. Each figure is composed of four graphs as follows:

- A) Individually fitted pF curves for particular soil samples (output of RETC);
- B) PTF-estimated pF curves using the equations by Wösten et al. (1998);

Table 7. R^2 coefficients for the correlation between parameters θ_s , α , and n derived by multiple regressions for particular sites and those obtained by fitting each curve individually

Site	Parameter	\mathbb{R}^2 coefficient (%)		
	θ_s	22.80		
Cerhovice	α	14.60		
	п	16.17		
	Θ_s	70.85		
Černičí	α	30.77		
	п	70.35		
	θ_s	7.20		
Brozany	α	7.64		
	п	1.72		
	Θ_s	11.43		
Ovesná Lhota	α	22.02		
	п	0.01		

- C) PTF-estimated pF curves using newly derived PTF's for particular sites;
- D) Comparison of pF curves A), B) and C) for a single selected soil sample.

The use of continuous parametric PTF's was tested on data from eight different sites in the Czech Republic. Unfortunately, the data sets were not large enough for an extensive study similar to the work by Wösten et al. (1998). No large data sets are presently available for the Czech Republic, because the Comprehensive Soil Survey database does not include virtually any retention curves, and the other data sources are scarce and difficult to identify. Therefore, a preliminary study was undertaken at the beginning of a more systematic effort in order to acquire experience with the continuous PTF's and their application to Czech data.

In general, the application of the original pedotransfer functions by Wösten et al. (1998), was not very successful. The most favorable values of RMSD ranged between 0.0591 and 0.0790, which corresponds with the results by Tietje and Tapkenhinrichs (1993). In other cases, however, the values of RMSD were much higher (see Table 6, column "Obs. vs. Wösten" for RMSD).

The newly derived pedotransfer functions, based on the data from all sites taken together and providing a rough estimate of the retention curve parameters θ_s , α^* and n^* , are presented in Table 5. Generally, they did not fit the observed retention curves very well. For some sites (Cerhovice, Džbánov, Podlesí and Žichlínek), the estimated curves corresponded quite well to the measured ones (RMSD ranging

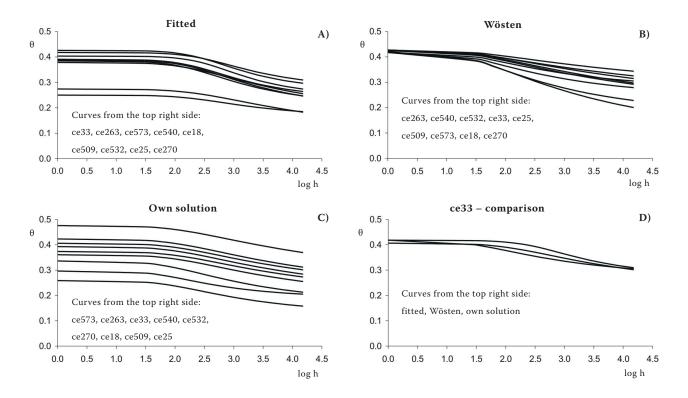


Figure 2. Cerhovice site – graphs of A) individually measured and fitted (using RETC) pF curves, B) pF curves derived from PTF's according to Wösten et al. (1998), C) pF curves from newly derived site-specific PTF's, D) comparison of A), B) and C) for a selected soil sample

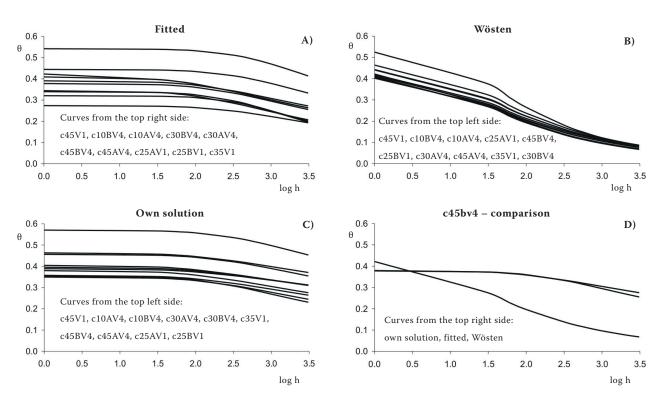


Figure 3. Černičí site – graphs of A) individually measured and fitted (using RETC) pF curves, B) pF curves derived from PTF's according to Wösten et al. (1998), C) pF curves from newly derived site-specific PTF's, D) comparison of A), B) and C) for a selected soil sample

between 0.0591 and 0.0790), but for the rest of the sites (Brozany, Černičí, Ovesná Lhota and Tupadly) the RMSD values were very high, which indicates poor agreement with the observed data.

For Brozany, Cerhovice, Černičí and Ovesná Lhota, site-specific pedotransfer functions were derived. The estimates for Cerhovice and Černičí were reasonably successful, RMSD being 0.0519 and 0.0451, respectively (Table 6), while for Brozany and Ovesná Lhota the RMSD values were very high. The Brozany soil, an artificial soil profile, is specific and its retention curves are difficult to reconcile with the van Genuchten's equation (1).

In general, the pedotransfer functions can be a useful tool to estimate the SMRC, but at least some SMRC have to be precisely measured for each soil type in order to derive a reliable SMRC. The use of PTF's in highly heterogeneous and man-made soils is disputable. The limiting and critical factors for deriving good PTF's are the quality and size of the input data sets.

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